
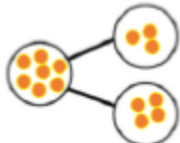
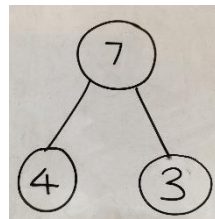
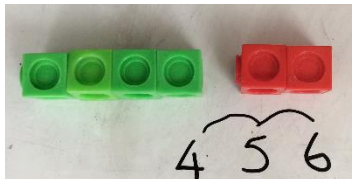
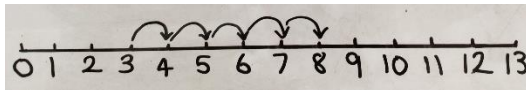
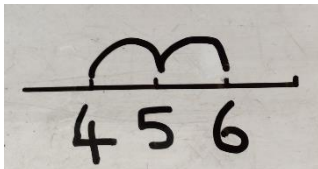
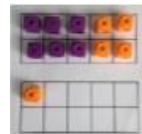

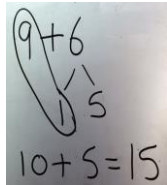


Hemingford Grey Calculation Policy

Concrete	Pictorial	Abstract				
Addition						
Foundation Stage and Key Stage 1						
<p>Combining two parts to make a whole $4+3=7$</p> 	<p>A group of 3 combined with a group of 4 makes 7</p> 	<p>$4+3=7$ (four is a part, 3 is a part and the whole is 7) You can show this on the 'cherry model' or the model'.</p> <table border="1" data-bbox="1411 595 1673 679"><tr><td colspan="2">7</td></tr><tr><td>4</td><td>3</td></tr></table>  'bar	7		4	3
7						
4	3					
<p>Counting on using cubes and number lines $4+2=6$</p> 	<p>$3+5=8$</p> 	<p>The abstract number line. What is 2 more than four? What is the sum of 4 and 2? What is the total of 4 and 2?</p> 				
<p>Regrouping to make 'friendly' 10 by using 10s frames and counters $6+5=11$ ("a 4 and a 1 live inside 5 and 6 add 4 will make a friendly 10" so $6+5$ becomes $10+1$)</p> 	<p>Children to draw the 10s frames and counters</p> 	<p>$9+6=15$ Inside 6 lives a 1 and a 5 so we can make a friendly 10 with the 9 and 1.</p> 				

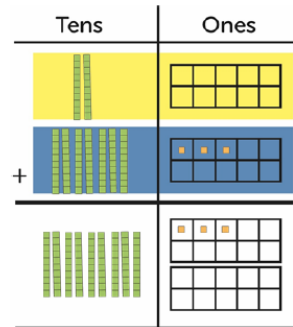
Hemingford Grey Calculation Policy

TO + O using dienes (T = tens and O = ones)

41+8



20+73

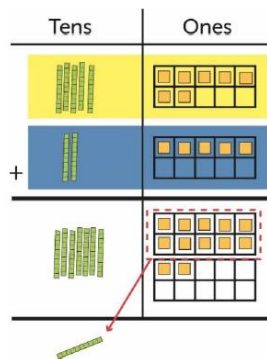


20+73

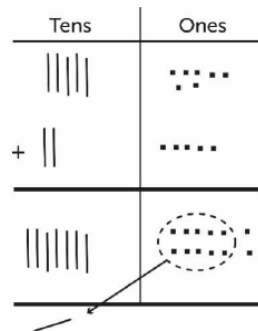
20	0
+ 70	3
90	3

TO + TO using dienes

57+25



57+25



57+25

50	7
+ 20	5
80	12 2
10	

7 + 5 = 12 but we need to put the 2 in the ones column and move the 10 to the tens column.
50+20=70 and then we must add the extra 10 to make 80.

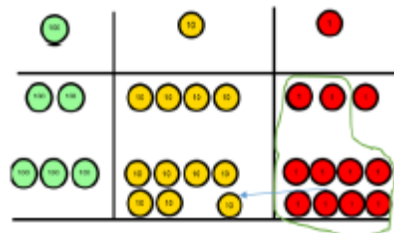
Hemingford Grey Calculation Policy

Key Stage 2

Use of place value counters to add HTO + HTU etc

243+368 (the 10 ones have been moved to make 1 ten. Then the 10 tens make another

100)



100s

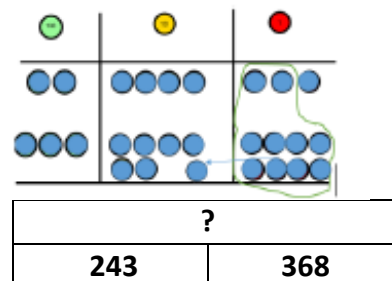
10s

1s

Concrete

Children to represent the counters:

If they are problem solving, draw a bar model to represent the problem.

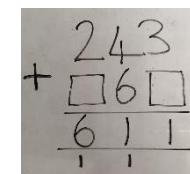


?=243+368

Pictorial

This written method can be used for larger numbers. Taking out some of the digits can be used for further challenge.

$$\begin{array}{r} 243 \\ +368 \\ \hline 611 \\ 1 \quad 1 \end{array}$$



Abstract

Subtraction

Foundation Stage and Key Stage 1

Physically taking away or removing objects from a whole.

4-3=1



Children to draw the concrete resource and cross it out.

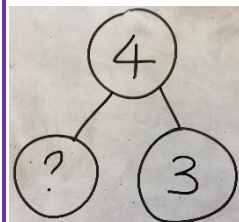
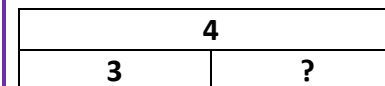


Use of the bar model:



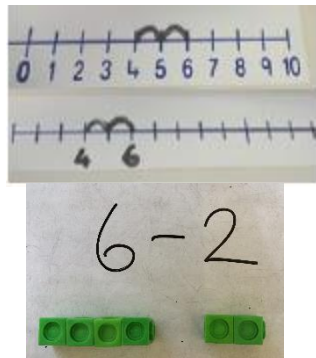
4-3

?= 4-3



Hemingford Grey Calculation Policy

Counting back (using a number line or track or cubes)



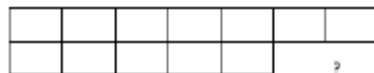
Find the difference (using cubes, Cuisenaire rods, or other objects)



Children to draw the concrete resources.
Find the difference between 9 and 5

XXXXXXXXXX
XXXXX

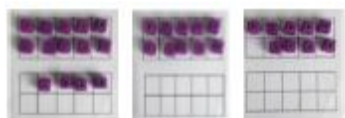
Use the model:



Find the difference between 8 and 6
8-6, the difference is?

Making "friendly 10" using ten frames.

14-5

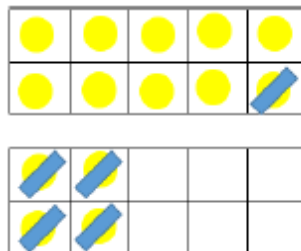


14-5=

14-4=10 (as inside 5 lives a 4 and a 1)

10-1=9

Children to represent the calculation



pictorially.

14-5

Cross out the 4
first to leave a
10 then cross
out the 1 from
the 10.

14-5=9 can be represented in the bar model.

14	
9	5

Children to represent different ways they have
solved the calculation.

Hemingford Grey Calculation Policy

Column Method (using dienes).

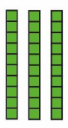

48-7

Children make the number using dienes and then physically remove 7 cubes.



35-4

Children cross out the ones

Tens	Ones
	

$$30 + 1 = 31$$

48-7

$$\begin{array}{r} 40 \quad 8 \\ - \quad \quad 7 \\ \hline \end{array}$$

Moving onto (in Key Stage 2):

874 – 523 becomes

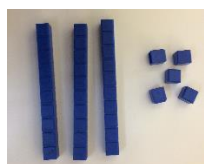
$$\begin{array}{r} 8 \quad 7 \quad 4 \\ - \quad 5 \quad 2 \quad 3 \\ \hline 3 \quad 5 \quad 1 \end{array}$$

Answer: 351

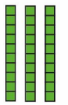

Exchanging using dienes or counters. 35-8

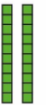

Children make the number out of dienes and then exchange 1 ten for 10 ones.

Make the number Exchange Take away the 8



35-8

Tens	Ones
	

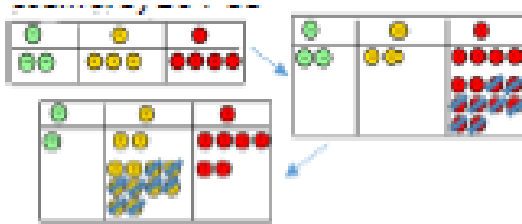
Tens	Ones
	

See below

Hemingford Grey Calculation Policy

Key Stage 2

Column Method using counters.
234-88



(the red counters represent ones, the yellow are tens and the green are hundreds. One of the tens is exchanged for 10 ones)

Children's own drawing of counters in a place value chart.

932 - 457 becomes With exchanging:

$$\begin{array}{r} 8 \quad 12 \quad 1 \\ 9 \quad 3 \quad 2 \\ - 4 \quad 5 \quad 7 \\ \hline 4 \quad 7 \quad 5 \end{array}$$

Answer: 475

Concrete

Pictorial

Abstract

Multiplication

Foundation Stage and Key Stage One

Repeated grouping or repeated addition.
3 times 4, 3 lots of 4 or 3 groups of 4



Children to represent the practical resources as a picture.

XX XX XX
XX XX XX

Use the bar model:



4x3
4+4+4

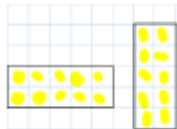
Hemingford Grey Calculation Policy

Use arrays to illustrate commutativity.

$2 \times 5 = 5 \times 2$



Children to draw the arrays and turn them round so they can see they represent the same total. 2×5 5×2



Children to be able to use an array to write a range of calculations.

$2 \times 5 = 10$


$5 \times 2 = 10$

$2 + 2 + 2 + 2 + 2 = 10$

$5 + 5 = 10$

Partition to multiply. (using dienes or place value counters)

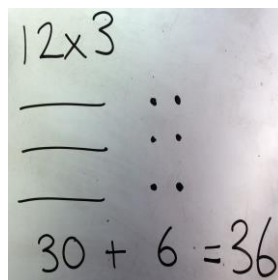
12×3 (12 "3 times" or 3 groups of 12)

tens	ones
	

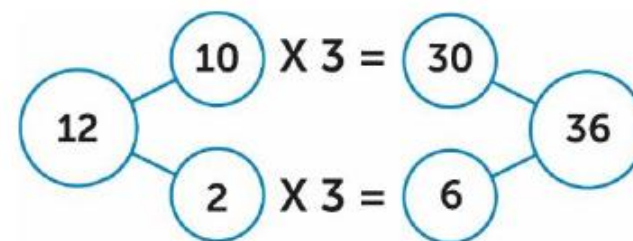
30

6

Children represent this pictorially



$12 \times 3 = 36$

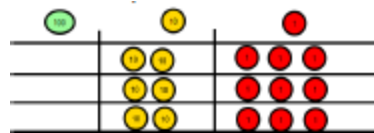


Hemingford Grey Calculation Policy

Key Stage 2

Formal column method. (using place value counters)

Make 23, 3 times



$$60 + 9 = 69$$

Children represent this pictorially

TH	H	T	O (1s)
	00	0	00
	00	0	00
	00	0	00
	00	0	00

1) $212 \times 4 = 848$ ✓

Short multiplication

Multiply 3×3 first,

Then 3×20

$$\begin{array}{r} 23 \\ \times 3 \\ \hline 69 \end{array}$$

$$6 \times 23 =$$

$$\begin{array}{r} 23 \\ \times 6 \\ \hline 138 \\ 11 \end{array}$$

342×7 becomes

$$\begin{array}{r} 342 \\ \times 7 \\ \hline 2394 \\ 21 \end{array}$$

Answer: 2394

A challenge could be removing a digit as above.

Hemingford Grey Calculation Policy

Long multiplication

6 x 124, then

20 x 124

$$\begin{array}{r}
 124 \\
 \times 26 \\
 \hline
 744 \\
 2480 \\
 \hline
 3224
 \end{array}$$

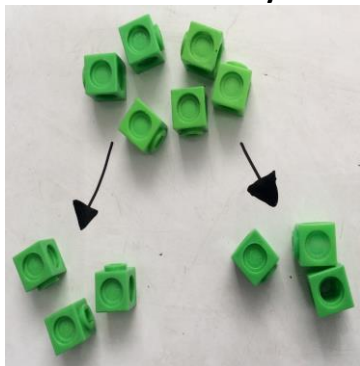
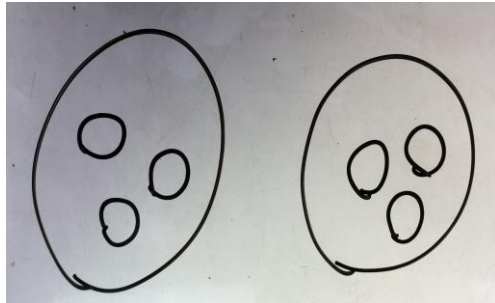
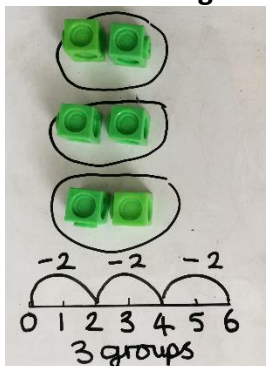
Answer: 3224

124 x 26 becomes

$$\begin{array}{r}
 124 \\
 \times 26 \\
 \hline
 744 \\
 2480 \\
 \hline
 3224
 \end{array}$$

Answer: 3224

Hemingford Grey Calculation Policy

Concrete	Pictorial	Abstract						
Division								
Foundation Stage and Key Stage 1								
<p>6 shared between 2. Sarah has 6 cubes and she shares them equally between herself and her friend Jo. How many do they have each?</p> 	<p>6 shared into 2 groups.</p> <table border="1"><tr><td>XXX</td><td>XXX</td></tr></table> 	XXX	XXX	<p>6÷2=3</p> <p>The bar model could be presented and the question asked: What’s the calculation?</p> <table border="1"><tr><td colspan="2">6</td></tr><tr><td>3</td><td>3</td></tr></table>	6		3	3
XXX	XXX							
6								
3	3							
<p>Understanding division as repeated grouping and subtracting. 6÷2</p> 	<p>There are 6 apples altogether but only 2 apples fit in each bag. How many bags do I need for all the apples?</p> <p>6 divided into groups of 3 with 2 in each group.</p> <p>XX XX XX</p>	<p>6÷2 3 groups of 2</p> <table border="1"><tr><td colspan="3">6</td></tr><tr><td>2</td><td>2</td><td>2</td></tr></table>	6			2	2	2
6								
2	2	2						
<p>Using a beadstring: Present children with a meaningful context</p>								

Hemingford Grey Calculation Policy

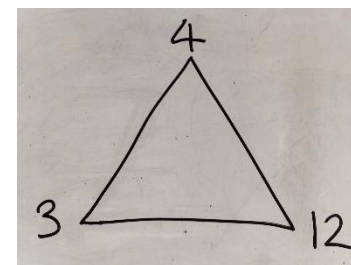
Each table in the picnic area could seat 5 children. Fifteen children were going to the picnic. How many tables would they need?

$$15 \div 5 = 3$$



Please note the links between \div and \times should be constantly reinforced. This can be done through the triangle model:

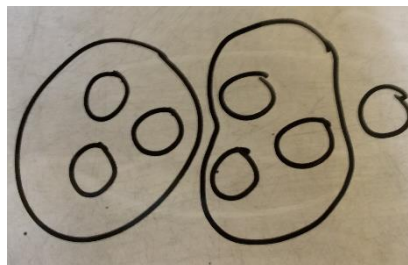
The core fact is $3 \times 4 = 12$ but we can derive a division fact from this.



$12 \div 4 = 3$ (the inverse)
and
 $12 \div 3 = 4$

Division with remainders

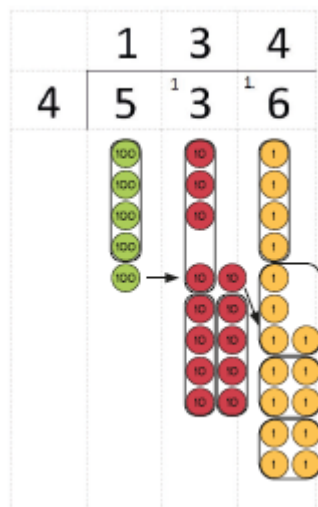
$$7 \div 2$$



$$7 \div 2 = 3r1$$

Key Stage 2

Grouping using place value counters



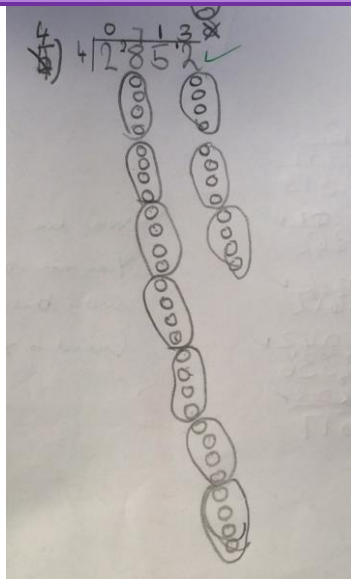
When I put 536 into groups of 4, I can see that there is 1 group of hundreds, 3 groups of tens and 4 groups of ones in 536.

There are $100 + 30 + 4$ groups of 4 in 536.

Each group will get 1 hundred (100), 3 tens (30) and 4 ones (4).

$$134 \times 4 = 536$$

$$536 \div 4 = 134$$



Short Division

$98 \div 7$ becomes

$$\begin{array}{r} 14 \\ 7 \overline{) 98} \\ \underline{7} \\ 28 \\ \underline{28} \\ 0 \end{array}$$

Answer: 14

$432 \div 5$ becomes

$$\begin{array}{r} 86 \text{ r } 2 \\ 5 \overline{) 432} \\ \underline{40} \\ 32 \\ \underline{30} \\ 2 \end{array}$$

Answer: 86 remainder 2

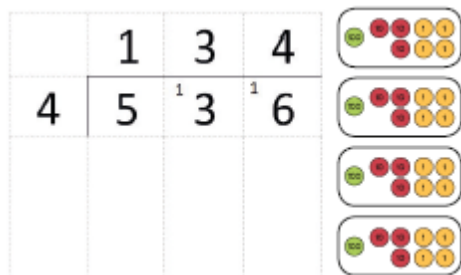
Hemingford Grey Calculation Policy

Division as sharing using place value counters

This is a division calculation. It is 536 shared equally by 4.

The counters represent 536 and they have been shared equally into the 4 boxes which were empty at the beginning. I want to know

how



many in each group.

Children represent the counters pictorially

Long Division

432 ÷ 15 becomes

$$\begin{array}{r}
 28 \text{ r } 12 \\
 15 \overline{) 432} \\
 \underline{30 } \\
 132 \\
 \underline{120} \\
 12
 \end{array}$$

432 ÷ 15 becomes

$$\begin{array}{r}
 28 \\
 15 \overline{) 432} \\
 \underline{30 } \quad 15 \times 20 \\
 132 \\
 \underline{120} \quad 15 \times 8 \\
 12
 \end{array}$$

432 ÷ 15 becomes ?

$$\begin{array}{r}
 28 \cdot 8 \\
 15 \overline{) 432 \cdot 0} \\
 \underline{30 } \quad \downarrow \\
 132 \\
 \underline{120} \quad \downarrow \\
 120 \\
 \underline{120} \\
 0
 \end{array}$$

Answer: 28.8

$$\frac{12}{15} = \frac{4}{5}$$

Answer: 28 $\frac{4}{5}$